

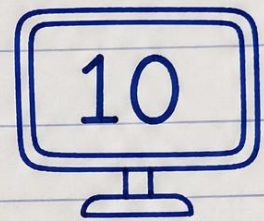
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Computer Fundamental Notes

Unit 6: Number System - Basics

Computer mein data ko represent karne ke liye Number System ka use hota hai. Iske main types hain:

Base-10



1. Decimal Number System:

Iska base 10 hota hai aur isme digits 0 se 9 tak use hoti hain.

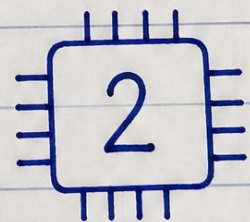
0 1 2 3 4
5 6 7 8 9

2. Binary Number System:

Iska base 2 hota hai aur isme sirf do digits 0 aur 1 hoti hain.

Computer internal data ko binary format mein hi process karta hai.

Base-2



0 1 0 1 1 0 1
1 0 1 0 0 1 0

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Unit 6: Number System - Dec-Bin Conversion

Conversions computer science mein
bohot important hain:

1. Decimal to Binary Conversion:

Decimal number ko 2 se divide
karte hain aur remainders ko
bottom-to-top likhte hain.

Example:

$$13 \text{ (base 10)} = 1101 \text{ (base 2)}$$

2. Binary to Decimal Conversion:

Binary digits ko 2 ki powers
se multiply karke add karte
hain taaki decimal value mil
sake.

Decimal to Binary Conversion

Division	Quotient	Remainder
2 13	6	1
2 6	3	0
2 3	1	1
2 1	0	1

↑
Stop

LSB
 ↑
 Read
 Bottom
 to
 Top
 ↓
 MSB

$$13 \text{ (base 10)} = 1101 \text{ (base 2)}$$

Example: 1101 (base 2)

Position (Right to Left)	Binary Digit	Power of 2	Multiplication
3	1	$2^3 = 8$	$1 \times 8 = 8$
2	1	$2^2 = 4$	$1 \times 4 = 4$
1	0	$2^1 = 2$	$0 \times 2 = 0$
0	1	$2^0 = 1$	$1 \times 1 = 1$

$$\text{Total} = 8 + 4 + 0 + 1 = 13$$

$$1101 \text{ (base 2)} = 13 \text{ (base 10)}$$

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Unit 6: Number System - Octal Conversion

1. Decimal to Octal Conversion:

Decimal number ko 8 se divide kiya jata hai aur remainders ko reverse order mein likhte hain.

Example:

$$100(\text{base } 10) = 144(\text{base } 8).$$

Decimal to Octal Conversion (Base-8)

		Remainder	
8	100	4	↑
8	12	4	↑
8	1	1	↑
	0	-	

Read remainders in reverse order → 144

2. Octal to Decimal Conversion:

Octal number ke har digit ko 8 ki powers (8^0 , 8^1 , 8^2 ...) se multiply karke sum nikalte hain.

Place Value Chart for Octal

Place (Power)	8^3	8^2	8^1	8^0
Value	512	64	8	1
Example (257) ₈	2	5	7	

$$\begin{aligned}
 (257)_8 &= 2 \times 8^2 + 5 \times 8^1 + 7 \times 8^0 \\
 &= 2 \times 64 + 5 \times 8 + 7 \times 1 \\
 &= 128 + 40 + 7 \\
 &= 175_{(10)}
 \end{aligned}$$

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Unit 6: Number System - Hex Conversion

1. Decimal to Hexadecimal Conversion:

- Decimal number ko 16 se divide karte hain; agar remainder 10-15 ho toh A-F use karte hain.

Example:

$$255_{(base\ 10)} = FF_{(base\ 16)}.$$

2. Hexadecimal to Decimal Conversion:

- Hex digits ko 16 ki powers se multiply karke decimal value calculate ki jati hai.

Hex to Decimal Reference (A-F)

Hex	Decimal
A	10
B	11
C	12
D	13
E	14
F	15

Decimal to Hexadecimal Example (255_{10})

$$\begin{array}{r} 16 \overline{) 255} \quad \text{Remainder} \\ \underline{160} \\ 15 \quad 15 (F) \uparrow \\ 16 \overline{) 15} \\ \underline{16} \\ 0 \quad 0 \uparrow \\ 16 \overline{) 0} \\ \underline{0} \\ 0 \quad 0 \uparrow \end{array}$$

Read remainder from bottom to top

$$255_{(base\ 10)} = FF_{(base\ 16)}$$

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Unit 6: Number System - Binary Arithmetic

Binary numbers ke sath arithmetic operations:

1. Binary Addition:

Rules:

- $0 + 0 = 0$
- $0 + 1 = 1$
- $1 + 0 = 1$
- $1 + 1 = 10$ (0 with carry 1)

Example:

$$101 + 011 = \underline{\underline{1000.}}$$

2. Binary Subtraction:

Rules:

- $0 - 0 = 0$
- $1 - 0 = 1$
- $1 - 1 = 0$
- $0 - 1 = 1$ (with borrow 1)

Binary Addition

Carry →	1	1	1
	1	0	1
+	0	1	1
	1	0	0

$$101 + 011 = \underline{\underline{1000}}$$

Binary Subtraction

Borrow →	1	1	1
	1	0	1
-	0	1	1
	0	1	0

$$101 - 011 = \underline{\underline{010}}$$

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Unit 6: Number System - Complements

1. 1s Complement:

Binary number ke sabhi 0s ko 1 aur 1s ko 0 mein convert karte hain.

Example:

$$1011 \rightarrow 0100$$

2. 2s Complement:

1s complement mein 1 add karne par 2s complement milta hai. Yeh negative numbers represent karne ke liye use hota hai.

Example:

$$1011 \rightarrow 0100_{(1s)} + 1 = 0101_{(2s)}$$

1s Complement (Inversion)

Rules: $0 \rightarrow 1, 1 \rightarrow 0$

$$\begin{array}{cccc} 1 & 0 & 1 & 1 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ 0 & 1 & 0 & 0 \end{array}$$

$$1011 \rightarrow 0100$$

2s Complement (Steps)

Step 1: 1s Complement lo.

$$\begin{array}{cccc} 1 & 0 & 1 & 1 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ 0 & 1 & 0 & 0 \end{array}$$

(1s Complement)

Step 2: Usme 1 add karo.

$$\begin{array}{cccc} & 0 & 1 & 0 & 0 \\ + & 0 & 0 & 0 & 1 \\ \hline & 0 & 1 & 0 & 1 \end{array}$$

(2s Complement)

$$1011 \rightarrow 0101$$

★ **Use:** 2s complement ka use computers mein subtraction aur negative numbers represent karne ke liye hota hai.